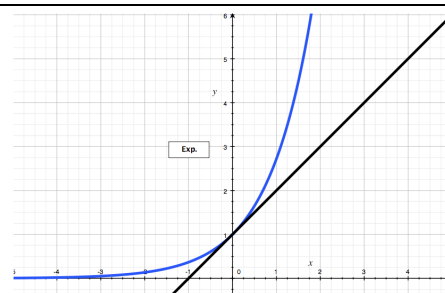
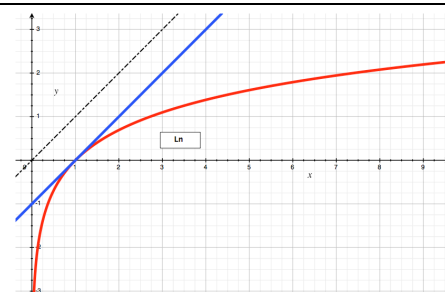


# Exponential – Power – Logarithm

## Limits and comparison of limits

I - Reminder :

|  |   |  |
|--|---|--|
| (1) $\lim_{x \rightarrow +\infty} \text{Exp}(x) = +\infty$ | (5) $\lim_{x \rightarrow +\infty} \ln(x) = +\infty$       |   |
| (2) $\lim_{x \rightarrow -\infty} \text{Exp}(x) = 0^+$     | (6) $\lim_{x \rightarrow -\infty} \ln(x) = \text{None !}$ |  |
| (3) $\lim_{x \rightarrow 0} \text{Exp}(x) = 1$             | (7) $\lim_{x \rightarrow 0^+} \ln(x) = -\infty$           |  |
| (4) $\lim_{x \rightarrow 0} \frac{e^x - 1}{x} = 1$         | (8) $\lim_{x \rightarrow 0} \frac{\ln(1+x)}{x} = 1$       |  |

II - Comparisons : ( $n \geq 2$ )

|   |  |   |
|---|--|---|
| (9) $\lim_{x \rightarrow +\infty} \frac{\text{Exp}(x)}{x} = +\infty$    | (13) $\lim_{x \rightarrow +\infty} \frac{\ln(x)}{x} = 0^+$     | (17) $\lim_{x \rightarrow +\infty} \frac{e^x}{\ln x} = +\infty$                   |
| (10) $\lim_{x \rightarrow +\infty} \frac{\text{Exp}(x)}{x^n} = +\infty$ | (14) $\lim_{x \rightarrow +\infty} \frac{(\ln(x))^n}{x} = 0^+$ | (18) $\lim_{x \rightarrow \pm\infty} x \cdot \ln\left(1 + \frac{1}{x}\right) = 1$ |
| (11) $\lim_{x \rightarrow -\infty} x \cdot \text{Exp}(x) = 0^-$         | (15) $\lim_{x \rightarrow 0^+} x \cdot \ln(x) = 0^-$           | (19) $\lim_{x \rightarrow 1} \frac{\ln(x)}{x-1} = 1$                              |
| (12) $\lim_{x \rightarrow -\infty} x^n \cdot \text{Exp}(x) = 0^\pm$     | (16) $\lim_{x \rightarrow 0^+} x \cdot (\ln(x))^n = 0^-$       | (20) $\lim_{n \rightarrow +\infty} \left(1 + \frac{1}{n}\right)^n = e$            |

***“The Exponential function imposes its limit to the Power”  
and “the Power function imposes its limit to the Logarithm function”***