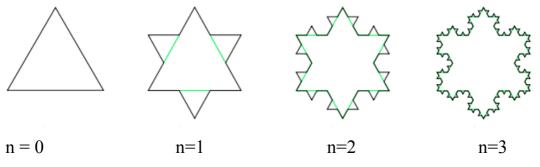
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## Geometric Series in Geometry (2) Von Koch's snow flake

## I. Construction of the basic pattern :

- 1. Divide the sides of an equilateral triangle into three equal parts
- 2. Erase the middle part of each side and replace it by an equilateral triangle
- 3. Do the same on each of the 4 new sides of the side ...



- **II. A paradoxal situation :** we want to show that the length of the curve goes to infinity, while the area inside has a finite limit.
  - i. Let's call  $P_n$  the length of the perimeter of the  $n^{th}$  picture
  - ii. Let's call  $C_n$  the number of sides

iii. Let's call  $A_n$  the area enclosed in the nth picture.

- **1.** Write P<sub>0</sub>, C<sub>0</sub>, A<sub>0</sub> (the length of the side of the initial triangle is 1 unit)
- **2.** Write P<sub>1</sub>, C<sub>1</sub>, A<sub>1</sub>, then P<sub>2</sub>, C<sub>2</sub>, A<sub>2</sub>:
- 3. Write the relationship between  $P_{n+1}$  and  $P_n$ ;  $C_{n+1}$  and  $C_n$ ;  $A_{n+1}$  and  $A_n$
- 4. Find the limits of each sequence  $(P_n)$ ,  $(C_n)$ ,  $(A_n)$ .