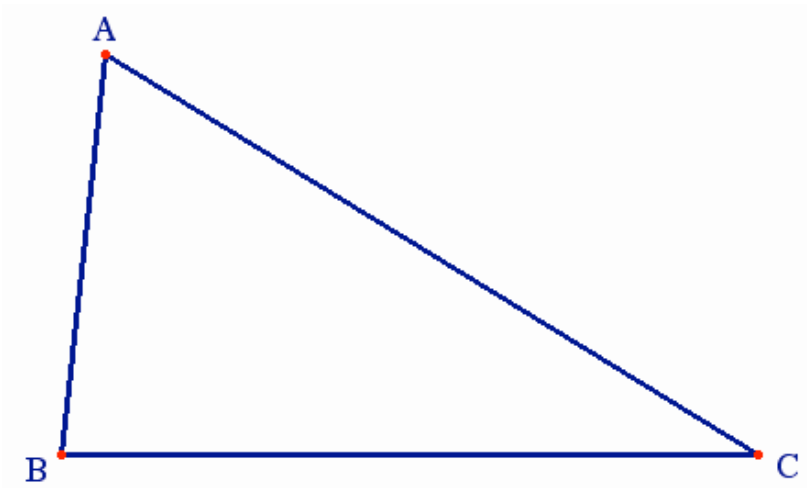
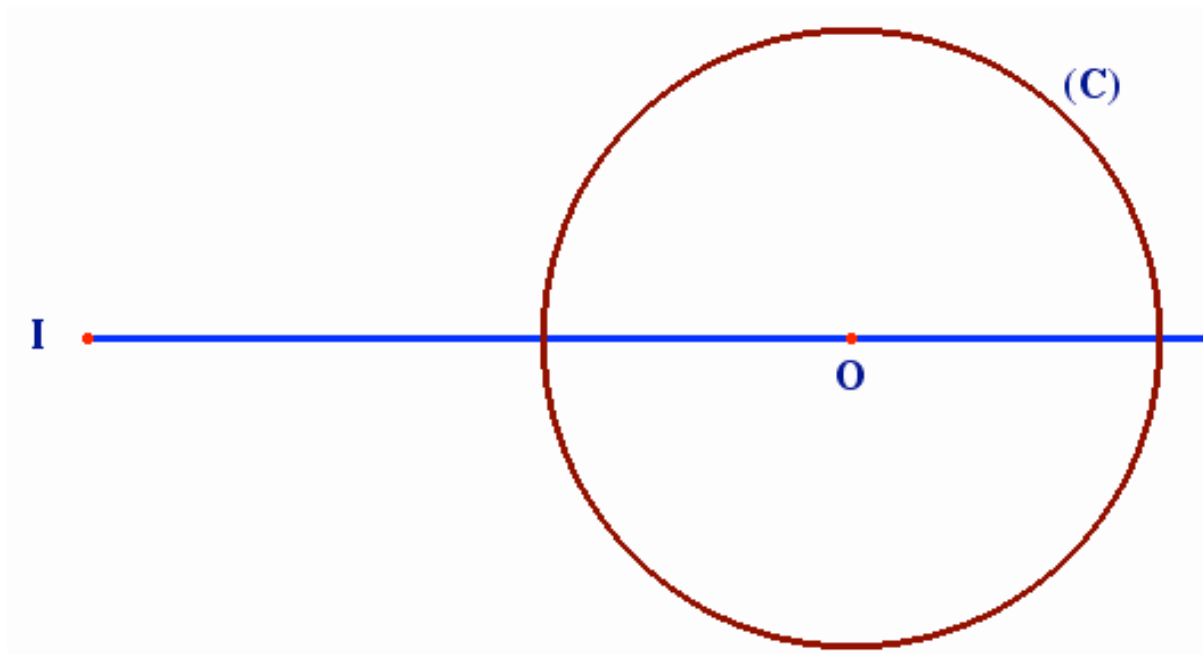


**Problem 1** : use a compass and a ruler to carefully build the circle inscribed in this triangle (*show the construction lines and explain your construction*).



**Problem 2** : given the circle (C), and a point I outside (C), use a compass and a ruler to carefully construct the two tangent lines to the circle from I. [*find the points K and K' on (C) so that the lines (IK) and (IK') be tangent to (C)*]

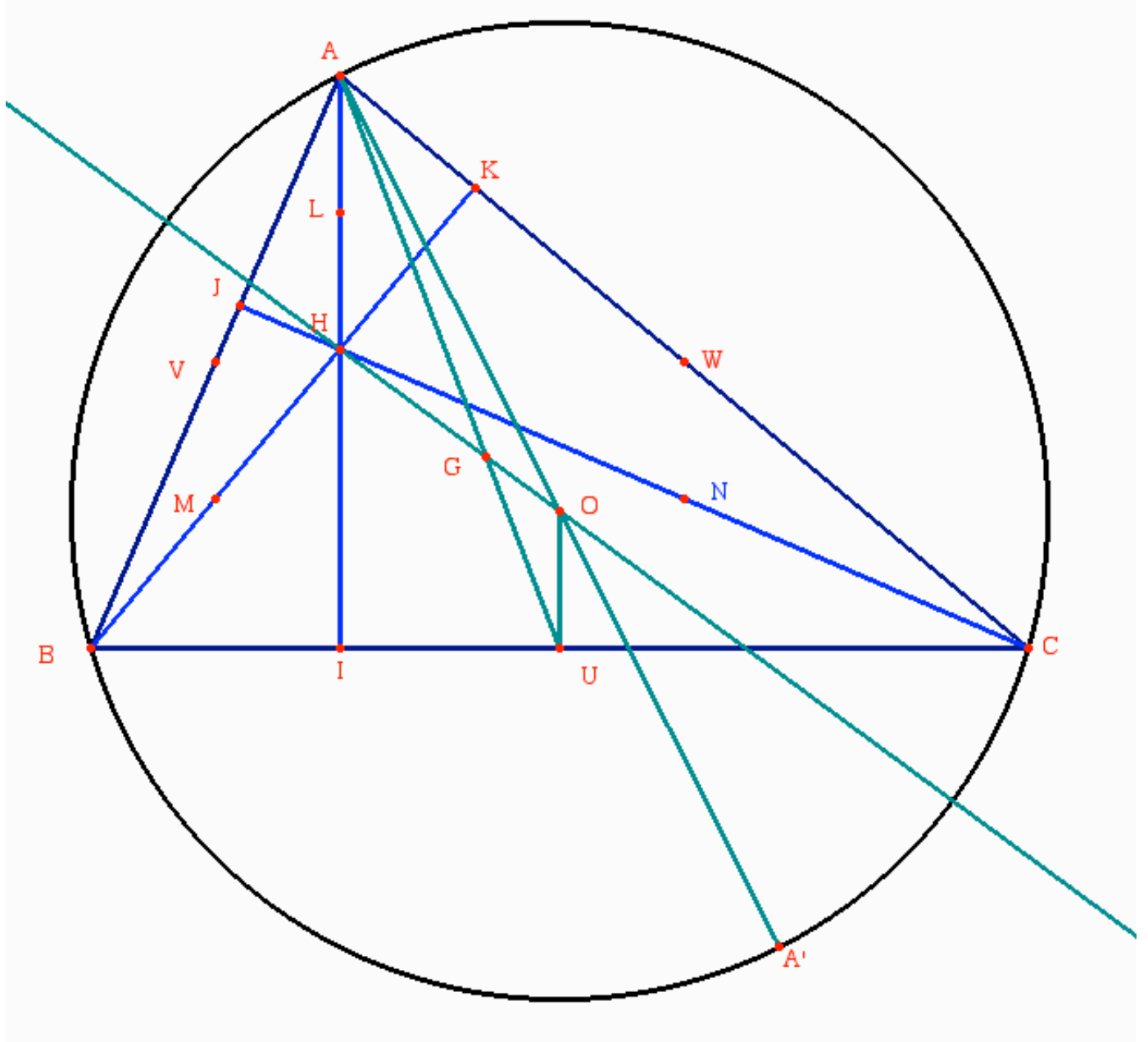


**Problem 3 :** given the triangle ABC, let H be the interception of its Heights, and O be the center of the circumscribed circle, U the middle of BC, and G the intersection of OH and AU.

1° Prove carefully (*on back of the page*) that  $GH = 2 GO$ .

2° Show why G is the center of gravity of the triangle.

[ *The line joining O,G,H is called Euler's line of the triangle*]



**Problem 4 :** given the triangle ABC, let H be the intercection of its Heights, and O be the center of the circumscribed circle, L the middle of AH, and P be the middle of OH.

- 1° Prove carefully (*on back of the page*) that  $PL = PU = PI$ .
- 2° By the same method prove that the circle centered in P and of  $r = R/2$  where R is the radius of (C), contains the 9 points : I,J,K,U,V,W,L,M,N (*this circle is named "Euler circle" of the triangle*)

