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## Euler＇s line proof by using vector calculations only．

Let ABC be a regular triangle， U the midpoint of $\mathrm{BC}, \mathrm{V}$ the midpoint of AB ，and W the midpoint of AC ．


1．Let M be the point defined by the vectorial equation $\overrightarrow{M A}+\overrightarrow{M B}+\overrightarrow{M C}=\vec{O}$
Show WHY this point M is the intersection $G$ of the three median lines AU，BV，CW．
2．Let N be the point defined by the vectorial equation $\overrightarrow{O A}+\overrightarrow{O B}+\overrightarrow{O C}=\overrightarrow{O N}$
Show WHY this point is the intersection H of the three heights AI，BK，CJ
3．From the above vectorial relations prove that $\mathrm{O}, \mathrm{G}, \mathrm{H}$ are on the same line（Euler＇s line）．

