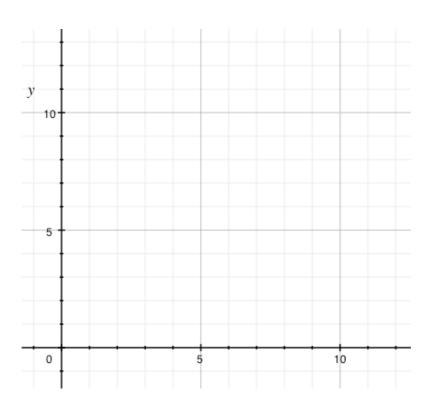
http://beijingshanmaths.org Name :	•	<i>Grade</i> :
jiguanglaoshi@gmail.com Junior 9	5 - Assign. #5 : Nov. 15 • .	2011 -p.1/2

## Numerical Sequences (2)

Problem I : Let f be the function defined by  $f(x) = \frac{1}{2}x + 4$  for  $x \ge 0$ .

Study the Sequence defined by the formula  $u_n = f(n) = \frac{1}{2}n + 4$  for every  $n \in \mathbb{N}$ .

- a. Graph the function f on  $[0; +\infty[$  and draw the first terms of the sequence  $(u_n)$ . Indicate from the graph whether or not the sequence is :
  - i. Monotonous (if yes how):
  - ii. Bounded (if yes, what are the boundaries?)
  - iii. Does-it seem to have a limit (if yes which one is it?)?
  - b. Prove that  $(u_n)$  is increasing
  - c. Explain why  $(u_n)$  is not bounded and goes to  $+\infty$



Problem II : Let f be the function defined by  $f(x) = \frac{1}{2}x + 4$  for  $x \ge 0$ .

Study of the sequence  $(v_n)$  defined by  $v_{n+1} = f(v_n) = \frac{1}{2}v_n + 4$ ;  $n \ge 1$  and  $v_0 = 3$ .

- 1. Graph the function f on  $[0; +\infty[$  and draw the first terms of the sequence  $(v_n)$ . Find the coordinates of the intersection of (Cf) with the first bisector (y = x) Indicate from the graph whether or not the sequence is:
  - i. Monotonous (if yes how):
  - ii. Bounded (if yes, what are the boundaries?)
  - iii. Does-it seam to have a limit, if yes which one can it be?
- 2. Let  $w_n = v_n 8$  for any n > 0.

Show that the new sequence  $(w_n)$  is a **geometric** sequence:

- 1. Find its first term and its reason.
- 2. Find the expression of  $w_n$  directly in function of n.
- 3. Deduct the limit of  $w_n$ .
- 4. Find the expression of  $v_n$  in function of  $w_n$
- 5. Find the limit of  $v_n$
- 6. For which value of n do we have  $7.999 < v_n < 8$

